

McInerney, James, Benjamin Lacker, Samantha Hansen, Karl Higley, Hugues Bouchard, Alois Gruson, and Rishabh Mehrotra. "Explore, exploit, and explain: personalizing explainable recommendations with bandits." In Proceedings of the 12th ACM Conference on Recommender Systems, pp. 31-39. ACM, 2018.

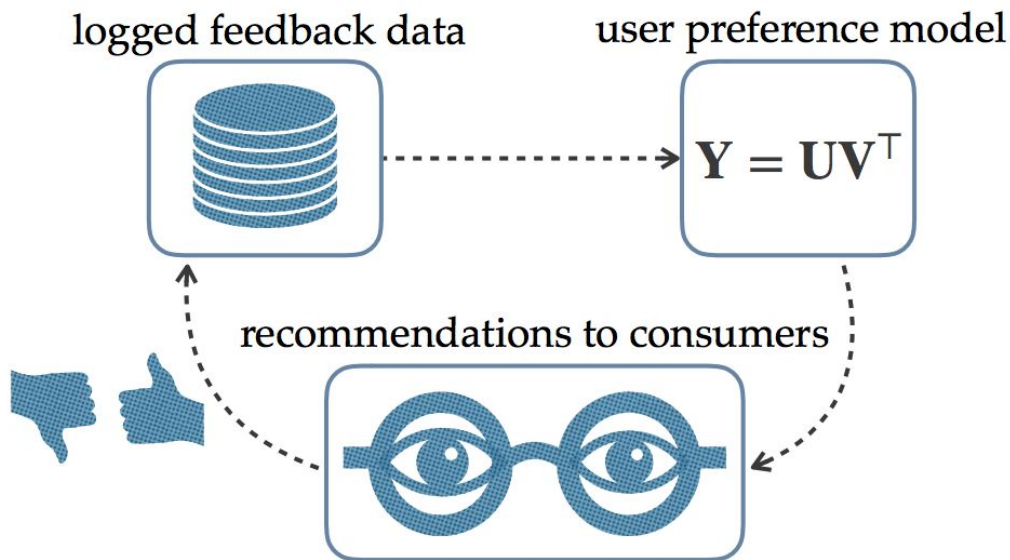
Slides

- Spotify
- Factorization Machine
- Epsilon-greedy
- IPS(inverse propensity score)

# Factorization Machine

$$r^{(2)}(j, e, x) = \sigma(\theta_{\text{global}} + \theta^\top x' + \sum_{a=1}^D \sum_{b>a}^D v_a^\top v_b x'_a x'_b) \quad (3)$$

# Collaborative filtering perpetuates the Pareto principle









“How Algorithmic Confounding in Recommendation Systems Increases Homogeneity and Decreases Utility” ([Chaney et al. 2017](#))

“Modeling User Exposure in Recommendation” ([Liang et al. 2016](#))

Standard collaborative filtering methods are limited because they can only exploit or ignore

**recommender system relevance certainty**

		Low certainty	High certainty
ground truth item relevance	Low relevance	 Sometimes Exploit  Sometimes Ignore	 Ignore
	High relevance	 Sometimes Exploit  Sometimes Ignore	 Exploit

# Exploration-Exploitation Policy & Propensity Scoring

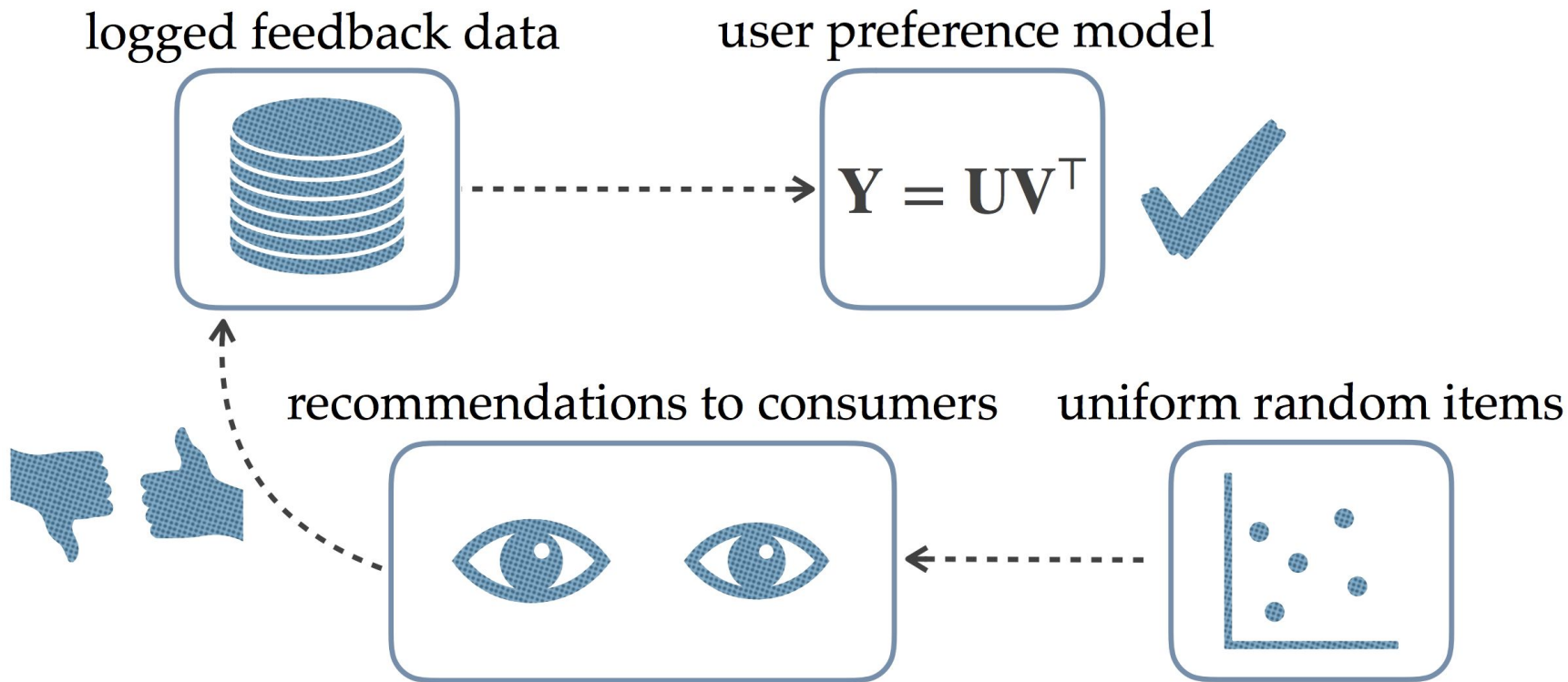
$$\pi_c^{\text{item}}(j | x, e) = \begin{cases} (1 - \epsilon) + \frac{\epsilon}{|f(e, u)|}, & \text{if } j = j^*, j \in f(e, x) \\ \frac{\epsilon}{|f(e, u)|}, & \text{if } j \neq j^*, j \in f(e, x) \\ 0, & \text{otherwise.} \end{cases}$$

$$\text{where } j^* = \arg_{j_1} \max r(j_1, e, x) \quad (7)$$

$$\pi_c^{\text{expl.}}(e | x, j) = \begin{cases} (1 - \epsilon) + \frac{\epsilon}{|\mathcal{E}|}, & \text{if } e = e^*, j \in f(e, x) \\ \frac{\epsilon}{|\mathcal{E}|}, & \text{if } e \neq e^*, j \in f(e, x) \\ 0, & \text{otherwise.} \end{cases}$$

$$\text{where } e^* = \arg_{e_1} \max r(j, e_1, x). \quad (8)$$

Let's restart from the basic ideal of randomized controlled trials



# Off-Policy Training

$$\hat{\theta}, \hat{v} = \arg_{\theta, v} \max \mathbb{E}_{A \sim \text{Uniform}(\cdot)} [\mathbb{E}_{X, R} [\log p_{\theta, v}(R|A, X)]] \quad (5)$$

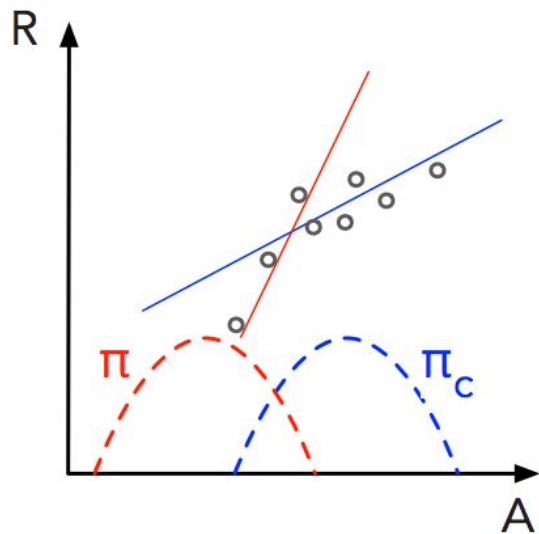
$$\approx \arg_{\theta, v} \max \frac{1}{N} \sum_{n=1}^N \frac{\text{Uniform}(a_n)}{\pi_c(a_n)} \log p_{\theta, v}(r_n|a_n, x_n). \quad (6)$$



IPS(inverse propensity score)



# Off-Policy Training



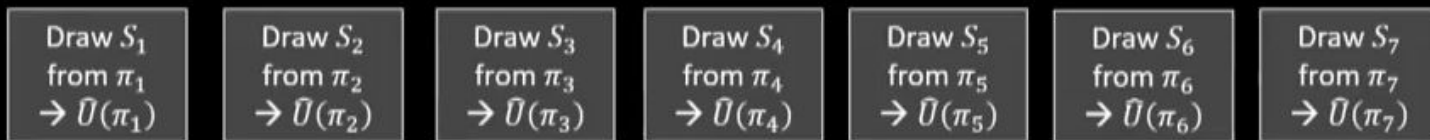
**Figure 3: Off-policy training fits a reward function that best fits the input points with respect to the target policy  $\pi$  using input points generated by the collection policy  $\pi_c$ .**

# Causal Inference Recommendation Papers

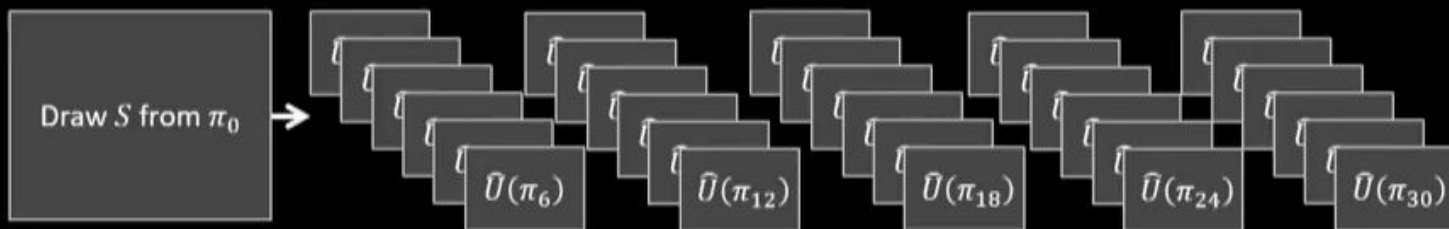
- Schnabel, Tobias, Adith Swaminathan, Ashudeep Singh, Navin Chandak, and Thorsten Joachims. "Recommendations as treatments: Debiasing learning and evaluation." arXiv preprint arXiv:1602.05352 (2016).
  - Propensity-Scored Matrix Factorization (= IPS + MF)
- Liang, Dawen, Laurent Charlin, and David M. Blei. "Causal Inference for Recommendation." (2016).
  - IPS + MF
- Bonner, Stephen, and Flavian Vasile. "Causal embeddings for recommendation." In Proceedings of the 12th ACM Conference on Recommender Systems, pp. 104-112. ACM, 2018.
  - Criteo, MF + Counterfactual Risk Minimization(CRM)
- Gilotte, Alexandre, Clément Calauzènes, Thomas Nedelec, Alexandre Abraham, and Simon Dollé. "Offline A/B testing for Recommender Systems." In Proceedings of the Eleventh ACM International Conference on Web Search and Data Mining, pp. 198-206. ACM, 2018.
  - Criteo, IPS
- Joachims, Thorsten, Adith Swaminathan, and Maarten de Rijke. "Deep learning with logged bandit feedback." (2018).
  - Unbiased estimate of risk => IPS
  - Partian Information => Variacne Control
  - Propensity Overfitting => SNIPS(self-normalized IPS estimator)

# Evaluating Online Metrics Offline

- Online: On-policy A/B Test



- Offline: Off-policy Counterfactual Estimates

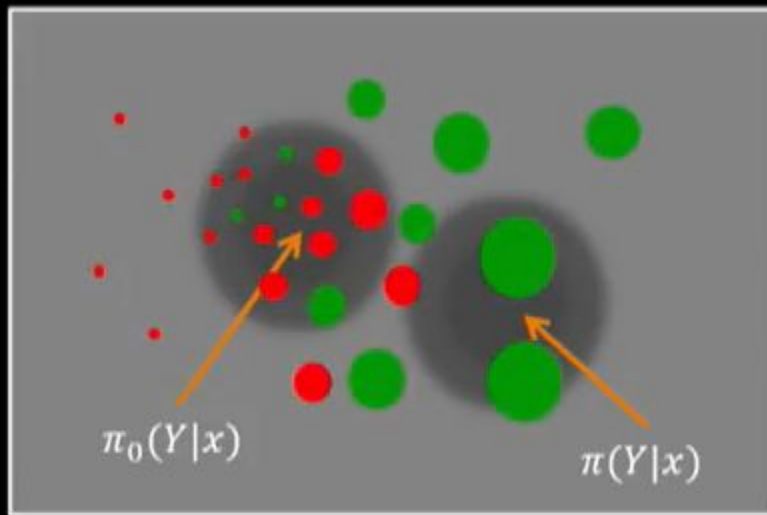


# Off-Policy Risk Evaluation

Given  $S = ((x_1, y_1, \delta_1), \dots, (x_n, y_n, \delta_n))$  collected under  $\pi_0$ ,

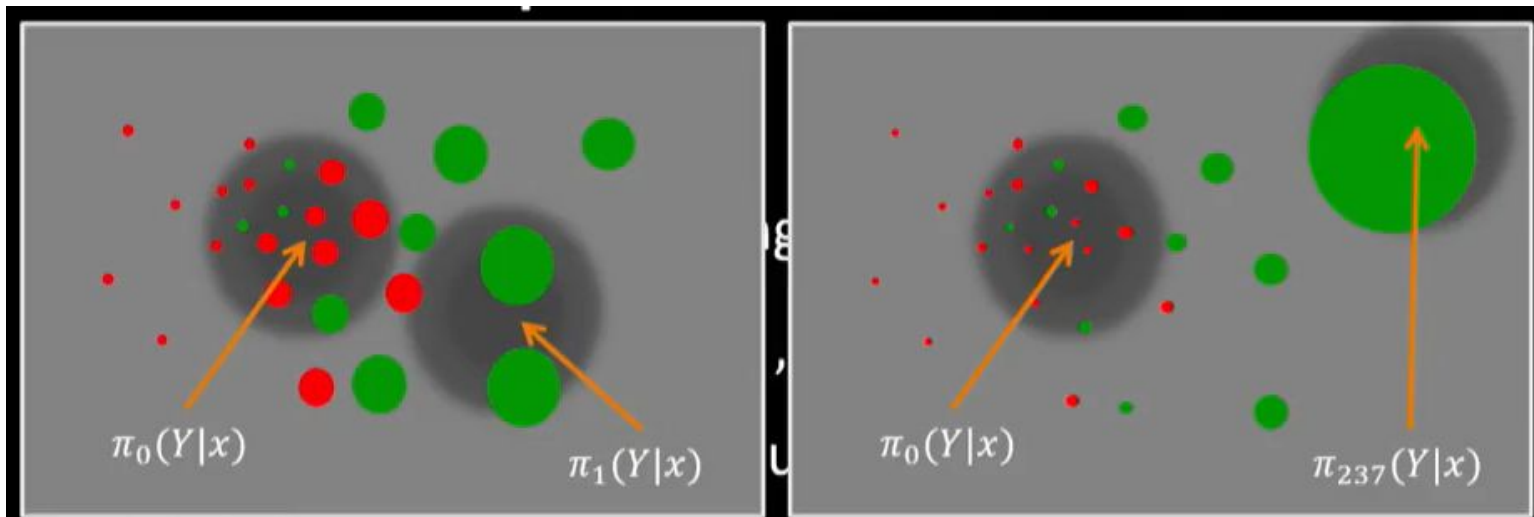
$$\hat{R}(\pi) = \frac{1}{n} \sum_{i=1}^n \delta_i \frac{\pi(y_i|x_i)}{\pi_0(y_i|x_i)}$$

Propensity  
 $p_i$



→ Unbiased estimate of risk, if propensity nonzero everywhere (where it matters).

# Partial Information Empirical Risk Minimization



- Training

$$\hat{\pi} := \operatorname{argmin}_{\pi \in \mathcal{H}} \sum_i^n \frac{\pi(y_i|x_i)}{p_i} \delta_i$$

# Variance Control

$$R(\pi) \leq \hat{R}(\pi) + O\left(\sqrt{\widehat{Var}(\pi)/n}\right) + O(C)$$

Unbiased  
Estimator

Variance  
Control

Capacity  
Control

$$\hat{R}(\pi) = \widehat{Mean}\left(\frac{\pi(y_i|x_i)}{p_i} \delta_i\right)$$

$$\widehat{Var}(\pi) = \widehat{Var}\left(\frac{\pi(y_i|x_i)}{p_i} \delta_i\right)$$

# Problem: Propensity Overfitting

- Example

- Training sample with losses:

	0	1	1	1	1	1
	1	1	1	0	1	1
	1	0	1	1	1	1
X	1	1	1	1	1	0
	1	1	0	1	1	1
	1	1	1	1	1	0
	1	1	1	0	1	1
	1	1	1	1	1	1

- Which  $\pi(y|x)$  minimize IPS?

$$R(\pi) = \min_{\pi \in H} \frac{1}{n} \sum_i^n \frac{\pi(y_i|x_i)}{p_i} \delta_i$$

# EQUIVARIANT COUNTERFACTUAL RISK MINIMIZATION

$$\hat{R}_{SNIPS}(\pi_w) = \frac{\frac{1}{n} \sum_{i=1}^n \delta_i \frac{\pi_w(y_i|x_i)}{\pi_0(y_i|x_i)}}{\frac{1}{n} \sum_{i=1}^n \frac{\pi_w(y_i|x_i)}{\pi_0(y_i|x_i)}}.$$



# TRAINING ALGORITHM

$$w = \operatorname{argmin}_{w \in \mathbb{R}^N} \left[ \hat{R}^{SNIPS}(w) + \lambda_1 \sqrt{\widehat{\operatorname{Var}}(\hat{R}^{SNIPS}(w))} + \lambda_2 \|w\|^2 \right]$$

# More about causal inference

- Ryan Tibshirani's lecture notes on causal inference
  - <http://www.stat.cmu.edu/~larry/=sml/Causation.pdf>
- Hernán, Miguel A. and James M. Robins. 2012. Causal Inference. Forthcoming, Cambridge University Press.
  - <https://www.hsph.harvard.edu/miguel-hernan/causal-inference-book/>